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( DEA)

TFP

Decision Making Unit

(DMU)

TFP

(Alirezaei et al. 2007) .

(Alirezaei et al. 2005) .

(DEA)

(Abbasiyan and Mehregan 2007) .

(DEA)

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DEA/AHP CEM A&P

(Safaie Qadyklaye et al. 2005) .

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Data Envelopment Analysis

.(Azar et al . 2005)

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(Farrell 1957)

$$u_{ro}, v_{io} \geq 0$$

$$i = 1, 2, \dots, n \quad r = 1, 2, \dots, s$$

$$j = 1, 2, \dots, m$$

$$0 \quad : u_{ro}$$

$$0 \quad : v_{io}$$

$$0 \quad : Y_{ro}$$

$$0 \quad : X_{io}$$

$$: Y_{rj}$$

$$: X_{ij}$$

$$: r, i, j$$

$r, i, j$  (Cooper)

(Edwardo)

(Charnes)

CCR

CCR (Charnes et al. 1978)

( )

Min  $\theta$

$$S.T \quad - \sum_{r=1}^s u_r Y_{ro} + \sum_{r=1}^s \lambda_r Y_{rj} \geq 0$$

$$\theta \sum_{i=1}^m v_i X_{io} - \sum_{i=1}^m \lambda_j X_{ij} \geq 0 \quad (2)$$

$$\lambda > 0$$

$$j = 1, 2, \dots, m$$

(Banker)

BCC

CCR

(Banker et al. 1984)

$$N \times 1 \quad \lambda$$

$$\theta$$

DEA

$$\theta \leq 1$$

CCR

$$MAX \quad \frac{\sum_{r=1}^s u_{ro} Y_{ro}}{\sum_{i=1}^n v_{io} X_{io}}$$

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$$S.T \quad \frac{\sum_{r=1}^s u_{ro} Y_{rj}}{\sum_{i=1}^n v_{io} X_{ij}} \leq 1$$

DEA

$$\text{Min } \theta$$

$$\text{S.t. } - \sum_{r=1}^s u_r Y_{ro} + \sum_{r=1}^s \lambda_j Y_{rj} \geq 0$$

$$\theta \sum_{i=1}^m v_i X_{io} - \sum_{i=1}^m \lambda_j X_{ij} \geq 0$$

$$\begin{aligned} NI'\lambda &\leq 1 \\ \lambda &> 0 \end{aligned}$$

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CCR

BCC DEA

CCR

CCR

BCC

DMU

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DMU

DMU

$$\text{Min } \theta$$

$$\text{S.t. } - \sum_{r=1}^s u_r Y_{ro} + \sum_{r=1}^s \lambda_j Y_{rj} \geq 0$$

$$\theta \sum_{i=1}^m v_i X_{io} - \sum_{i=1}^m \lambda_j X_{ij} \geq 0 \quad ( )$$

$$NI'\lambda = 1$$

$$\lambda > 0$$

DMU

DMU

$$Max D_k$$

$$s.t :$$

$$-D_k Y_{11} + (Y_{11}\lambda_1 + Y_{21}\lambda_2 + \dots) \geq 0$$

$$\dots$$

$$-D_k Y_{1j} + (Y_{1j}\lambda_1 + Y_{2j}\lambda_2 + \dots) \geq 0 \quad ( )$$

$$X_{11} - (X_{11}\lambda_1 + X_{21}\lambda_2 + \dots) \geq 0$$

$$X_{li} - (X_{li}\lambda_1 + X_{2i}\lambda_2 + \dots) \geq 0$$

$$\lambda_t \geq 0$$

$$t = 1, 2, 3, \dots$$

K DMU

=D

=  $\lambda$

DMU

j

=Y<sub>li</sub>

DMU

i

=X<sub>li</sub>

CCR

BCC

DEA

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## References

Abbasiyan, A. and Mehregan, N., 2007. measured Total factors productivity the country's economic sectors by method data envelopment analysis, *Economic Research Spring*., pp.153-176. [In Persian].

Adel, A., Anvar Rostami, A.A. and Rostami, M.R., 2005. Measuring the relative efficiency of the company present in stock exchange covering data

analysis approach (information technology indices); *Studies of accounting and auditing*, Winter: **14**(50): pp: 119-138 [In Persian].

Alirezaei, MR., Afsharian, M. and Analuyi B., 2007. Calculated total factor productivity growth models to help Non paramtric method data envelopment analysis; a case study in the power

- industry, *Economic Research Spring* (78), pp :177-206 [In Persian].
- Alirezaei, MR., Keshvari, A. and Hashemi, SM., 2005. evaluate productivity growth index analysis envelopment Malmkuyist approach, *International Journal of Engineering Sciences, Summer*; **16**(2) pp:145-154 [In Persian].
- Banker, RD., Charnes, A. and Cooper, WW., 1984. Some Models For Estimating Technical Scale Efficiencies in Envelopment Analysis. *Management Science*. **30**(9), pp. 1078-1092.
- Charnes, A., Cooper, WW. and Rhodes, E., 1978. Measuring the Efficiency of Decision Making Units. *European Journal of operational Research*, **2**, pp. 429-444.
- Farrell, M., 1957. The Measurement of Productive Efficiency. *Journal of the Royal Statistics Society ,SeriesA*, **120**(3), pp. 253-281.
- Safaie Qadyklayy, A., born Far, M. and Shokouhi, B., 2005. Investment companies measure performance using data envelopment analysis (DEA) in Tehran Stock Exchange, *Journal of Humanities and Social Summer*, **7**(25), (Special Management), pp:97-120 [In Persian].